

Suppression and recovery of the ferroelectric phase in multiferroic MnWO_4

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We report the discovery of a complete suppression of ferroelectricity in MnWO_4 by 10% iron substitution and its restoration in external magnetic fields. The spontaneous polarization in $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ arises below 12 K in external fields above 4 T. The magnetic and/or ferroelectric phase diagram is constructed from the anomalies of the dielectric constant, polarization, magnetization, and heat capacity. The observations are qualitatively described by a mean-field model with competing interactions and strong anisotropy. We propose that the magnetic field induces a noncollinear inversion symmetry breaking magnetic structure in $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$.

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I. INTRODUCTION

Multiferroic materials in which ferroelectric (FE) and magnetic orders coexist and mutually interact have recently attracted attention because of many novel physical phenomena observed in these compounds as well as their potential for applications as magnetoelectric sensors or memory chips.^{1,2} Common features and magnetoelectric properties of compounds with quite different chemical compositions and structures indicate a universal physical mechanism behind the multiferroic phenomena of a large materials class. It was shown that a noncollinear (or helical) spin density wave can break the spatial inversion symmetry and, with sufficiently strong spin-lattice coupling, can result in a lattice distortion with a FE polarization.³ The helical magnetic order was in fact observed in the FE phases of TbMnO_3 ,⁴ $\text{Ni}_3\text{V}_2\text{O}_8$,⁵ MnWO_4 ,⁶ etc. Most multiferroics exhibit highly frustrated magnetic orders due to geometric constraints or competing interactions. Local lattice distortions can therefore release the magnetic frustration, lower the magnetic energy, and induce local electrical dipoles that may add up to a macroscopic polarization if permitted by symmetry.⁷ In frustrated magnetic systems, several magnetic states are close in energy and compete for the ground state. As a result, in multiferroic systems, the FE polarization, which is induced by magnetic order, is easily controlled by small perturbations affecting the microscopic exchange constants or the magnetic order. For example, it was shown that magnetic fields^{6,8-10} and external pressure¹¹⁻¹³ have a significant effect on the ferroelectric polarization and the multiferroic properties.

The multiferroic MnWO_4 passes through three magnetic transitions upon decreasing temperature T . The sinusoidal AF3 phase ($12.6 < T < 13.5$ K) is followed by a noncollinear helical spin phase AF2 ($7.8 < T < 12.6$ K), both phases with an incommensurate (IC) modulation vector $\vec{q}_{2,3} = (-0.214, 1/2, 0.457)$. The AF1 phase below 7.8 K is collinear [$\vec{q}_1 = (\pm 1/4, 1/2, 1/2)$] and shows the typical $\uparrow\uparrow\downarrow$ (E type) spin pattern.¹⁴ Ferroelectricity was only observed in the helical AF2 phase,^{6,15} but Heyer *et al.* reported a finite value of the FE polarization also in the low temperature AF1 commensurate phase.¹⁶ However, our recent polarization mea-

surements of MnWO_4 at ambient and high pressures¹³ are consistent with the paraelectric nature of the AF1 phase. Magnetic frustration due to competing exchange interactions and a strong uniaxial anisotropy lead to the sequence of complex magnetic structures. Tuning the magnetic exchange interactions appears to be imperative to arrive at a deeper understanding of the multiferroic properties of MnWO_4 and related compounds. The superexchange interactions depend on the type of magnetic ions, their interatomic distances, and bond angles. The remarkable sensitivity of the FE and magnetic phases of multiferroic materials with respect to hydrostatic pressure was demonstrated for MnWO_4 ,¹³ $\text{Ni}_3\text{V}_2\text{O}_8$,¹¹ and RMn_2O_5 ,¹² proving the high susceptibility of multiferroics to small perturbations. Alternatively, magnetic exchange interactions can be controlled by replacing one kind of magnetic ions with other ions, either nonmagnetic or with different magnetic properties. In MnWO_4 , the magnetic Mn^{2+} ion with spin $S=5/2$ can easily be replaced by the Fe^{2+} ion with a smaller magnetic moment ($S=2$) and different exchange and anisotropy constants. In an attempt to examine the detailed interplay between magnetic interactions and ferroelectricity, we have therefore investigated the solid solution $\text{Mn}_{1-x}\text{Fe}_x\text{WO}_4$. We found that $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ is paraelectric (PE) in zero magnetic field at all temperatures; however, ferroelectricity and multiferroic properties are induced by magnetic fields above 4 T.

II. METHODOLOGY

Polycrystalline $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ was synthesized by solid state reaction at 930 °C of the precursor compounds Mn_2O_3 , WO_3 , and Fe_2O_3 , mixed in the appropriate ratios. Single crystals have been grown from the polycrystalline feed rod in a floating zone furnace. X-ray analysis showed the monoclinic structure with lattice constants $a=4.799(2)$ Å, $b=5.736(2)$ Å, and $c=4.980(2)$ Å, in good agreement with previous reports on natural and synthetic Wolframites.^{17,18} The crystals have been characterized and oriented by single crystal Laue diffractometry. The homogeneity of the crystals and their Fe content were verified by wavelength dispersive spectroscopy analysis. Magnetic measurements were con-

ducted in a superconducting quantum interference device in magnetic fields up to 5 T. For the dielectric constant and polarization measurements a homemade dielectric probe was adapted to the physical property measurement system (PPMS) for temperature and magnetic field ($H < 7$ T) control. The crystals were shaped as thin parallel plates, the dielectric constant was calculated from the capacitance measured by the high-precision AH2500A capacitance bridge, and the polarization was determined by integrating the pyroelectric current measured by a K6517A electrometer. During the pyroelectric measurements, a small poling electric field was applied in order to align domains in the ferroelectric state. The PPMS was also used for heat capacity measurements at temperatures above 1.8 K in different magnetic fields.

III. EXPERIMENTAL RESULTS

The low-field magnetization data are consistent with previous reports¹⁹ and they reveal two successive phase transitions at $T_N=15.4$ K and at $T_L=12$ K, respectively, in excellent agreement with the phase diagram of $Mn_{1-x}Fe_xWO_4$ for $x=0.1$ previously derived from neutron scattering experiments.¹⁸ According to the neutron data, magnetic order sets in at T_N with an IC modulation vector $\vec{q}_3 = (-0.235, 1/2, 0.49)$, similar to the AF3 phase of pure $MnWO_4$. At T_L , the magnetic modulation locks into a commensurate order described by $\vec{q}_1 = (\pm 1/4, 1/2, 1/2)$ (AF1 phase of $MnWO_4$). The spins are oriented along the easy axis in the ac plane at an angle of 35° with the a axis.

A. Dielectric constant and polarization

In order to search for the signature of ferroelectricity, we have performed measurements of the dielectric constant $\varepsilon(T)$ and the pyroelectric current along all three crystallographic orientations. In zero magnetic field, we did not find any indication of a FE transition, in contrast to the ferroelectricity observed in $MnWO_4$.⁶ Minute changes of slope of $\varepsilon(T, H=0)$ near T_N and T_L are barely visible in the inset of Fig. 1. The replacement of 10% Mn by Fe apparently leads to the complete loss of ferroelectricity and, presumably, the loss of the helical magnetic structure in the compound. This conclusion is supported by the results of neutron scattering experiments that did not show an intermediate phase between T_N and T_L in zero magnetic field.

In external magnetic fields H_e , oriented along the magnetic easy axis, however, new anomalies in the dielectric properties, measured along the monoclinic b axis, could be observed. In the following we discuss dielectric and polarization data measured along the b axis in external fields H_e . With increasing magnetic field a distinct peak of $\varepsilon(T)$ develops near the lock-in transition temperature T_L . The peak appears for fields exceeding about 4 T and increases with H_e (inset of Fig. 1). The pyroelectric current also exhibits a sharp peak, indicating the onset of FE order at T_L . The results for the polarization $P(T)$ at different magnetic fields are shown in Fig. 1. At 4.5 T, close to T_L , $P(T)$ is small but it increases significantly at about 6 K, indicating a major

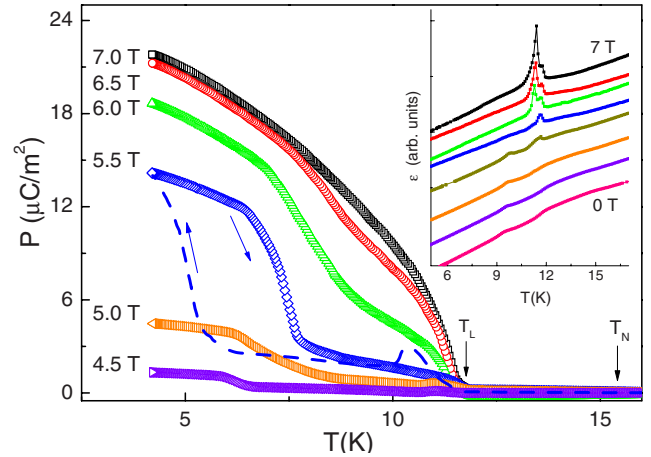


FIG. 1. (Color online) Polarization $P(T)$ of $Mn_{0.9}Fe_{0.1}WO_4$ in different fields above 4 T (cooling data included at 5.5 T as dashed line, while all other data are shown for increasing T). Inset: $\varepsilon(T)$ for fields from 0 to 7 T (curves are vertically offset).

change within the ferroelectric phase from a low-polarization (LP) to a high-polarization (HP) state. Similar transitions within the ferroelectric phase have been observed in other multiferroic compounds and are sometimes attributed to spin reorientations associated with a change of the FE polarization.⁷ The $P(T)$ data also reveal a large temperature hysteresis, as shown for $H_e=5.5$ T in Fig. 1. With increasing magnetic field, $P(T)$ increases quickly, and at 7 T, the FE polarization increases continuously from T_L toward lower T . From the $\varepsilon(T)$ and $P(T)$ data shown in Fig. 1, we conclude that $Mn_{0.9}Fe_{0.1}WO_4$ is paraelectric at zero magnetic field but ferroelectricity is induced by fields above 4 T.

In order to further study the field-induced FE phase, we have conducted field-dependent isothermal polarization measurements. The results (Fig. 2) unambiguously prove the ferroelectricity arising above a critical magnetic field. The transition into the FE phase exhibits a field hysteresis of more than 0.5 T (inset of Fig. 2) confirming the first-order nature

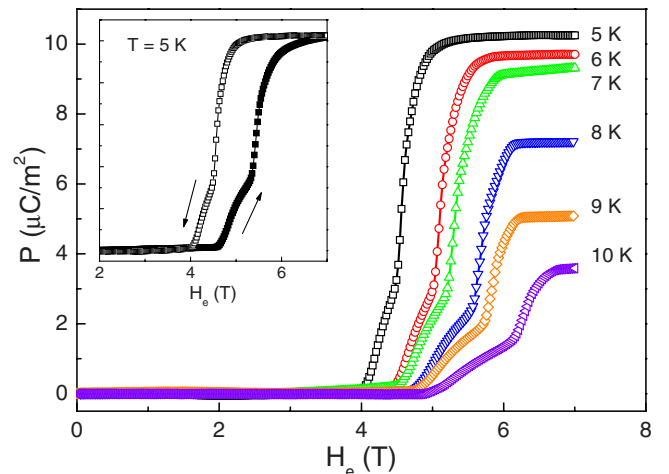


FIG. 2. (Color online) Isothermal field dependence of the FE polarization (data shown for decreasing field only). Inset: 5 K data with increasing and decreasing field.

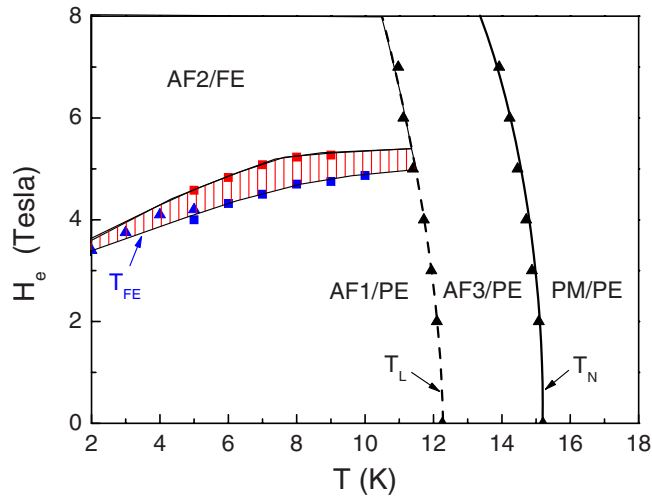


FIG. 3. (Color online) Magnetic phase diagram of $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ with H along the easy axis. The FE phase is labeled AF2/FE. Data are from polarization (squares) and magnetization (triangles) measurements. T_{FE} was determined from $P(H)$ and $M(H)$. The shaded area indicates the field hysteresis of the FE transition.

of this phase transition. $P(H)$ shows a characteristic kink which is consistent with the sudden increase of $P(T)$ from the LP to the HP state, as discussed above. The origin of this distinct feature is not clear and has yet to be investigated. From these data, a field-temperature phase diagram for $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ is constructed and shown in Fig. 3 (the hysteresis across the ferroelectric transition is shown as the dashed area). The field dependence of the Néel temperature (T_N) and the lock-in temperature (T_L) are derived from magnetic and heat capacity measurements (discussed below). Both temperatures decrease slightly with H_e as expected for an antiferromagnetic (AFM) state. At low fields, T_N and T_L define the transitions PM/PE \rightarrow AF3/PE \rightarrow AF1/PE. The field-induced FE phase is labeled as AF2/FE.

B. Magnetic properties

The ferroelectricity in most multiferroic compounds is strongly coupled to the magnetic order. Therefore, any change of the dielectric state should also be detected as anomalies of the magnetic properties. The magnetization measurements of $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ shown in Fig. 4 indeed reflect the major phase transitions observed in dielectric and polarization measurements. At the Néel temperature $M(T)$ exhibits the characteristic maximum with the onset of IC AFM order. $M(T)$ shows a subtle change with a temperature hysteresis of about 2 K at T_L . This hysteresis indicates the first-order nature of the lock-in transition. In high magnetic fields and at low temperature, $M(T)$ reveals another distinct anomaly with a wide hysteresis similar to the polarization data shown in Fig. 1. The change of the magnetic order at the high-field FE transition is also detected in the $M(H)$ measurements (inset of Fig. 4). The sharp increase of $M(H)$ above 4 T and the observed hysteresis suggest that the magnetic order undergoes a major modification. Note that the

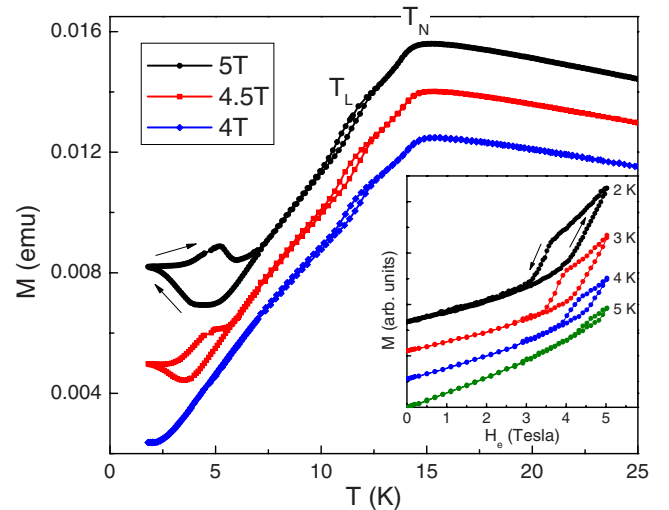


FIG. 4. (Color online) High-field magnetization M of $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$. The loop at low T indicates the transition into the AF2/HP phase. Inset: $M(H_e)$ at different temperatures (data for $T < 5$ K are vertically shifted).

maximum field of the magnetometer (5 T) is not enough to complete the transition into the high-field phase; however, the critical fields and temperatures derived from the decreasing field cycle (triangles in Fig. 3) agree well with the similar data from the $P(H)$ measurements (squares in Fig. 3). We conclude that the magnetic field along the easy axis induces a new magnetic order that breaks the spatial inversion symmetry and is compatible with the FE order. Any other direction of the magnetic field was found to be less or not at all efficient in stabilizing the FE phase. We have also extended the pyroelectric measurements along the a and c axes at zero and high magnetic fields but we did not find any signature of FE order along these orientations.

C. Heat capacity

The thermodynamic signature of transitions between different phases or orders is usually detected in distinct anomalies of the heat capacity, $C_p(T)$. Multiferroic materials with a sequence of subsequent transitions may show more or less pronounced sudden changes of C_p , some can be subtle and difficult to detect.⁷ Figure 5 shows the heat capacity data, C_p/T , for $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ in different external magnetic fields H_e . For $H_e=0$, a sharp increase of $C_p(T)$ at T_N indicates the onset of the IC sinusoidal order. At the lock-in transition, C_p exhibits a sharp peak which is difficult to resolve in detail because of the strong first-order nature of this transition. No significant field dependence of C_p/T is noted up to 3 T. The only change in this low-field range is a small shift of the steplike increase at T_N and the peak at T_L toward lower T . At higher magnetic fields, however, C_p/T shows a well resolved enhancement below the critical temperature of the ferroelectric order (indicated by dashed arrows in Fig. 5). This anomaly quickly shifts to higher T with increasing H_e and it merges with the lock-in temperature T_L at the highest field (7 T in Fig. 5). The enhanced heat capacity is a clear thermodynamic signature of the ferroelectric order in the

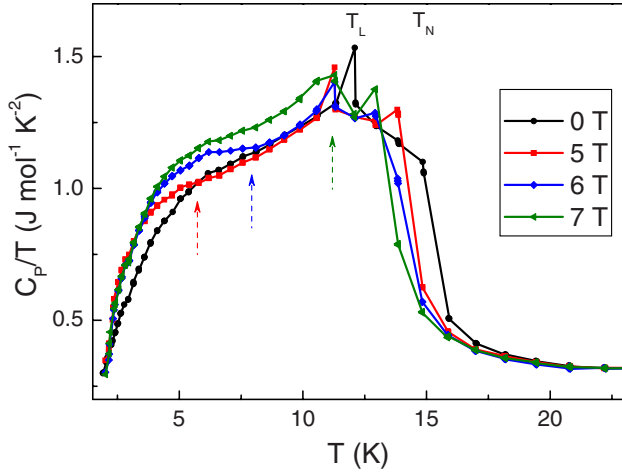


FIG. 5. (Color online) Heat capacity C_p/T of M of $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ at zero and high magnetic fields (field along the easy axis). The dashed vertical arrows point to the anomaly associated with the ferroelectric transition at 5, 6, and 7 T, respectively (left to right).

AF2/FE phase and it proves the bulk nature of the FE high-field phase.

IV. MODEL CALCULATIONS

Ferroelectricity induced by a magnetic field is a rare phenomenon and it shows the sensitivity of the frustrated magnetic system toward small perturbations. A simple model describing the different magnetic structures (commensurate $q = 1/4$ at $T=0$, IC helical and sinusoidal orders at $T>0$) has to include the competing exchange interactions, the magnetic anisotropy, and the external field (\vec{H}). It should be noted that the spin order in the low-temperature commensurate phase of MnWO_4 can be represented by a stack of spin chains in the ac plane with equal spin values within each chain but a four-fold modulation ($q=1/4$) of moments perpendicular to the chains. The order of spin chains is then described by the characteristic $\uparrow\uparrow\downarrow\downarrow$ (E type) modulation.¹⁴ Within a simplified description, we can describe the major features of the magnetic order by a mean-field model of spin chains stacked along one dimension with effective exchange coupling and anisotropy parameters.

The Heisenberg model with competing nearest (J_1) and next-nearest-neighbor interactions (J_2) and spin anisotropy (K) interpolates between the helical ground state (isotropic model)²⁰ and the E -type ($\uparrow\uparrow\downarrow\downarrow$) modulation for strong uniaxial anisotropy (Ising limit).²¹ A similar model has been employed to describe qualitatively the magnetic phase sequence in $\text{Ni}_3\text{V}_2\text{O}_8$.²² For simplicity, we consider the $S=1$ model with the easy axis of magnetization along the z direction,

$$H = J_1 \sum \vec{S}_n \vec{S}_{n+1} + J_2 \sum \vec{S}_n \vec{S}_{n+2} - K \sum (S_n^z)^2 - \vec{H} \sum \vec{S}_n, \quad (1)$$

which includes the most basic parameters and interactions to describe the various spin orders in $\text{Mn}_{1-x}\text{Fe}_x\text{WO}_4$ and other

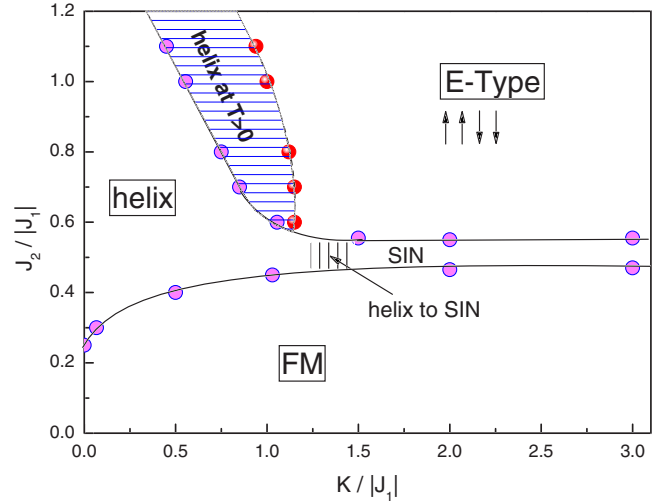


FIG. 6. (Color online) Ground state phase diagram of model (1) in mean-field approximation.

multiferroics. Neutron scattering experiments on MnWO_4 suggest a competition between ferromagnetic (FM) ($J_1 < 0$) and AFM ($J_2 > 0$) exchange interactions and a strong uniaxial anisotropy ($K > 0$), favoring the spin orientation along the easy axis in the ac plane.¹⁴ Model (1) is solved in the mean-field approximation. In this approximation, the two-spin interaction is replaced by a single-spin term in an effective field of the neighboring spins that is proportional to the corresponding exchange coupling constants and the thermal average of the spins at nearest or next-nearest neighbor sites. The thermodynamic average of all spins is then calculated self-consistently from a set of N coupled equations, with N being the total number of spins along the chain. For simple commensurate spin orders, the set of N equations can be reduced to a smaller number of equations assuming translational symmetry of the average spin values according to the specific order. For example, for a two-sublattice antiferromagnetic order the self-consistency equations are reduced to two coupled equations, one for each sublattice. However, in the case of arbitrary (commensurate or incommensurate) magnetic orders, no assumption about the periodicity of the magnetic order can be made and a large set of N coupled equations has to be considered. We solve the mean-field equations for finite lattices of up to 100 spins assuming periodic boundary conditions. The solution of the mean-field equations for a given set of parameters (K, J_1, J_2, T , or magnetic field) without any initial constraints on the magnetic order reproduces the different magnetic structures observed in $\text{Mn}_{1-x}\text{Fe}_x\text{WO}_4$ and MnWO_4 , E type, and sinusoidal (IC) collinear, as well as IC helical spin modulations. Wherever more than one type of order was obtained self-consistently from the equations, the solution with the lower free energy was determined as the stable magnetic configuration.

The ground state phase diagram of Eq. (1) for zero field is shown in Fig. 6. At $K=0$, the ground state is FM for $J_2/|J_1| < 1/4$ and it assumes the noncollinear (NC) incommensurate spin structure for larger J_2 . For large K , the Ising limit is reproduced and the transition from FM to the collinear E -type magnetic order takes place at $J_2/|J_1| = 1/2$ as in

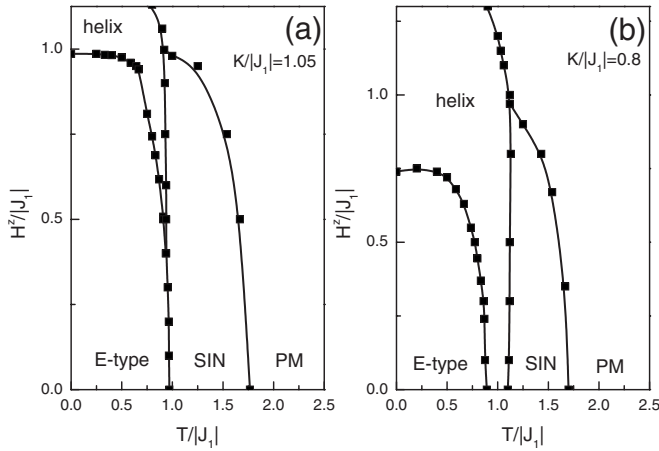


FIG. 7. Field-temperature phase diagrams for model parameters qualitatively describing the phase sequence in (a) $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ and (b) MnWO_4 .

the Axial Next-Nearest Neighbor Ising model.²¹ The E -type phase is stable for larger J_2 and K and the NC helical phase covers the left section of the ground state phase diagram. For $J_2/|J_1| \approx 1/2$, the helical spin component perpendicular to the easy axis rapidly decreases with increasing K and it disappears at the transition into the collinear sinusoidal structure close to $K/|J_1| \approx 1.25$ (vertically dashed area in Fig. 6). The horizontally dashed area in Fig. 6 marks the region of special interest. Within this area, the NC helical spin order appears at finite temperatures between the E -type ground state and the sinusoidal phase. This phase sequence is typical for MnWO_4 . With increasing K , however, the helical phase becomes unstable at all T and, with increasing temperature, the transition proceeds directly from the E -type state to the sinusoidal phase, as observed for $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$. The lack of ferroelectricity (at zero field) in $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ is therefore explained by the increase of the uniaxial anisotropy K . Evidence for the increase of K with Fe substitution was also derived from the results of neutron scattering experiments.^{18,19} The chosen set of parameters, $J_2 \approx |J_1|$, results in a spin modulation in the IC phase, $Q_{SIN} = 0.21$, that is comparable with the experimental results.^{14,20}

In order to understand the magnetic field induced ferroelectricity in $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$, we have to consider model (1) in fields oriented along the easy axis (z axis) and search for NC (helical) spin structures. The solution of Eq. (1) in the mean-field approximation for parameters $J_1 = -1$, $J_2 = 1$, $K = 1.05$, and $\vec{H} = (0, 0, H^z)$ indeed reveals a magnetic field induced transition from the E -type order to a NC helical phase at low temperatures. The H^z - T phase diagram for this case is shown in Fig. 7(a). At zero magnetic field the phase sequence with increasing T is E type \Rightarrow SIN \Rightarrow PM but above a critical field the helical spin structure is stabilized as an intermediate phase. The helical and the sinusoidal phases are incommensurate with a modulation comparable to the experimental results. It is remarkable that the simple model [Eq. (1)] describes the main physical effects of the Fe sub-

stitution, namely, (i) the loss of the FE (helical) phase with the increase of the anisotropy (Fe substitution) and (ii) the reappearance of this phase above a critical magnetic field oriented along the easy axis of magnetization. For lower anisotropy ($K=0.8$), the known magnetic phase diagram¹⁵ for MnWO_4 is qualitatively reproduced, as shown in Fig. 7(b). Note that the sinusoidal spin order is also suppressed by H^z in agreement with the experimental results for MnWO_4 . The phase transitions from the E type to sinusoidal and helical phases (Fig. 7) are first-order transitions, whereas a second-order transition takes place from the sinusoidal to the paramagnetic phase, in accordance with our experimental results discussed above.

V. SUMMARY AND CONCLUSIONS

We have shown that the ferroelectric and helical magnetic orders in MnWO_4 are easily suppressed by replacing only 10% of the magnetic Mn^{2+} ion by another magnetic ion, Fe^{2+} . The ferroelectric state is restored in external magnetic fields applied along the easy axis of the spins. We have resolved the field-temperature phase diagram for $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ showing three distinct magnetic and/or ferroelectric phases. The experimental observations are explained by a mean-field solution of the Heisenberg model with competing interactions, uniaxial anisotropy, and external magnetic field. The destruction of the ferroelectric and/or helical phase is due to an increase of the uniaxial anisotropy with the iron substitution. The calculated phase diagrams describe the experimental results for $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ and MnWO_4 qualitatively well. While the model is too simple to allow for any quantitative comparison with the experiments, it includes the major physical interactions to describe qualitatively the different magnetic phases in MnWO_4 and $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$. Improvements of the model description should include the three-dimensional lattice structure and spin order, the differences in the exchange coupling constants between Mn and Fe ions, and the effects of disorder. The results of our simple model calculation should also be relevant to other multiferroic materials such as CuFeO_2 where magnetic field induced ferroelectricity has been observed very recently.^{23,24} Our experimental results and calculations for $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$ suggest that with increasing magnetic field the collinear E -type spin modulation turns into a helical IC magnetic order breaking the spatial inversion symmetry which allows for the observed ferroelectricity. This transition could be verified by high-field neutron scattering experiments. It is expected that these experiments also reveal additional details of the magnetic orders within the FE phase as observed by us in $\text{Mn}_{0.9}\text{Fe}_{0.1}\text{WO}_4$. Large single crystals are currently being grown for further investigations.

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